ACTIVITY RATIOS OF LYATE IONS IN THE WATER-ALCOHOL MIXTURES

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A new method for calculating the activity ratio of lyate ions in the water-alcohol mixtures is proposed on the basis of utilizing the linear relations between the Gibbs energies of ion transfer. The results for the water-methanol, -ethanol, and -2-propanol systems are compared with literature data. At the same time, the individual ionic products of water and alcohol in their mixtures were calculated. The accuracy of the method depends on the accuracy of experimental determination of the Gibbs energies of electrolyte transfer and of ionic products in mixed solvents.

In the binary mixtures of water (W) and alcohol (ROH), the ionic product, K_s , can be expressed by the relation^{1,2}

$$K_{\rm S} = a_{\rm H^+}(a_{\rm OH^-} + a_{\rm RO^-}) = K_{\rm W} + K_{\rm ROH} = K_{\rm W}(1 + Q_1), \qquad (1)$$

where a_{H^+} is the proton activity, a_{OH^-} , a_{RO^-} are the activities of hydroxide and alkoxide ions in the given mixture S, K_W and K_{ROH} are the individual ionic products of water and alcohol in the mixture, Q_1 is the ratio of activities of alkoxide and hydroxide ions. Unfortunately, the individual ionic products K_W , K_{ROH} , and/or ratio Q_1 are not direct experimentally measurable quantities. For some special cases of binary mixtures (in pure solvents), constants K_1 were determined for the equilibrium of lyate ions²⁻¹⁰. They are defined by the relation

$$K_1 = (a_{\rm RO} - a_{\rm H_2O}) / (a_{\rm OH} - a_{\rm ROH}) = Q_1 a_{\rm H_2O} / a_{\rm ROH}$$
(2)

but these constants were hitherto not determined experimentally and are along with K_w , K_{ROH} , and ratio Q_1 accessible only by calculating.

Gaboriaud and co-workers¹¹ suggested a solution of this problem for the water--methanol mixtures by introducing an empirical equation for the dependence of ionic product on the mixture composition from which it is possible to calculate the ratio of activities of lyate ions Q_1 . By extending this method to the water-ethanol, -1-propanol, and -2-propanol mixtures has not been so successful⁹ because the

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analogous empirical equations have described the dependence of ionic product on the mixture composition at most up to 50 mass % of organic component.

Another procedure for the same system of mixed solvents was proposed by Rochester². The ionic product of water and ionic product of methanol change with increasing methanol concentration. To express the dependence of ionic products of both the components on the mixture composition, he proposed two methods. The first one assumes that the activity coefficients of methoxide and hydroxide ions are a linear function of methanol mole fraction. The second one is based on the assumption that the Gibbs energies of transfer of methoxide and hydroxide ions are a linear function of the average Gibbs energy of transfer of halide ions (Cl⁻, Br⁻, I⁻). The results of both the methods are comparable and are as well comparable with those reported by Gaboriaud and co-workers¹¹. A deficiency, however, consists in the applicability of both the methods only to 80 mass % methanol and a considerable dependence on the way of determining $\Delta G_t^0(\text{ion})$ for halide ions¹². On extending the Rochester methods to the mixtures of water with ethanol and 2-propanol, the results obtained were of limited validity⁹ only.

Considering that the calculation of activity ratio of lyate ions and/or individual ionic products has hitherto been carried out only for the water-methanol mixture, it is therefore probable that the considered assumptions for this calculation are not of a general validity. This contribution shows the possibility of a new method for calculating the activity ratio of lyate ions, Q_1 , in binary mixtures of water and alcohol.

Principle of the Method

For the experimentally obtained Gibbs energies of transfer from a standard solvent (conventially is chosen water¹³) into the given solvent S, ΔG_t^0 (electrolyte), it is assumed that they are additive¹⁴, i.e., equal to the sum of $\Delta G_t^0(anion) + \Delta G_t^0(cation)$. This assumption follows from the requirement of choice of standard state as an infinitely diluted solution of the given electrolyte in an arbitrary solvent S where no interactions between cations and anions are considered any more.

Let, in the given solvent S, the Gibbs energies of transfer be known for electrolytes containing all combinations of $A_1, A_2, ..., A_n$ anions and $K_1, K_2, ..., K_m$ cations, that means altogether $(n \times m)$ values of ΔG_t^0 (electrolyte) which can be arranged in the matrix form.

Matrix (3) describes the experimentally accessible values of Gibbs energies of

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transfer of electrolyte in the given solvent S but at the same time it is evident that not all values in it are independent. The number of independent quantities (i.e., the base of the given system) is equal to the rank of matrix (3) which can be determined in the following way:

- the first column is subtracted from the other (n - 1) columns,

- the first row is subtracted from the other (m - 1) rows.

Matrix (4) of rank 2

$$\begin{bmatrix} \Delta G_{t}^{0}(\mathbf{K}_{1}) + \Delta G_{t}^{0}(\mathbf{A}_{1}) \ \Delta G_{t}^{0}(\mathbf{A}_{2}) - \Delta G_{t}^{0}(\mathbf{A}_{1}) \dots \Delta G_{t}^{0}(\mathbf{A}_{n}) - \Delta G_{t}^{0}(\mathbf{A}_{1}) \\ \Delta G_{t}^{0}(\mathbf{K}_{2}) - \Delta G_{t}^{0}(\mathbf{K}_{1}) & 0 & \dots & 0 \\ \vdots & \vdots & \vdots \\ \Delta G_{t}^{0}(\mathbf{K}_{m}) - \Delta G_{t}^{0}(\mathbf{K}_{1}) & 0 & \dots & 0 \end{bmatrix}_{s}$$
(4)

results from these rearrangements, which means that also the initial matrix (3) has therefore rank 2 and therefore, in given solvent S, the arbitrary Gibbs energy of transfer of electrolyte, ΔG_t^0 (electrolyte), is a linear function of two others. It is evident from matrix (4) as well that there exist linear relations between columns or rows which can be written in the general form

$$\Delta G_{t}^{0}(\mathbf{A}_{i}) - \Delta G_{t}^{0}(\mathbf{A}_{j}) = \alpha(ijk)_{s} \left[\Delta G_{t}^{0}(\mathbf{A}_{k}) - \Delta G_{t}^{0}(\mathbf{A}_{j}) \right], \qquad (5)$$

$$\Delta G_{t}^{0}(\mathbf{K}_{i}) - \Delta G_{t}^{0}(\mathbf{K}_{j}) = \beta(ijk)_{s} \left[\Delta G_{t}^{0}(\mathbf{K}_{k}) - \Delta G_{t}^{0}(\mathbf{K}_{j}) \right], \qquad (6)$$

where $\alpha(ijk)_s$, $\beta(ijk)_s$ are proportionality factors. Both the relations satisfy as well the first requirement of linear dependence between the Gibbs energies of electrolyte transfer on the assumption that the electrolytes have a common cation (Eq. (5)) or anion (Eq. (6)).

All the procedure was carried out for the case of univalent anions and cations. The extension for polyvalent ions, however, does not make substantial difficulties. The most important problem of applicability of these equations is the behaviour of coefficients $\alpha(ijk)_s$ and $\beta(ijk)_s$ in dependence on a change of solvent S which cannot be explained on the basis of thermodynamics. However, on the assumption that there exist linear relations between solvation energies or there exist some extrathermodynamic relations describing the dependence of $\Delta G_t^0(ion)$ on solvent (an extensive discussion was carried out by Kamlet and co-workers¹⁴), $\alpha(ijk)_s$ and $\beta(ijk)_s$ will be constant in all solvents S, which means that Eqs (5) and (6) have the same form for the given anions A_i , A_j , A_k or for the given cations K_i , K_j , K_k in all solvents. The advantage of relations defined in this way is their independence of the estimate of ionic contribution $\Delta G_t^0(ion)$ because their differences are experimentally measurable, and the independence of the choice of definition (molar. molal, or rational).

In such a way defined relations can be used for estimating the activity ratio of

lyate ions Q_1 . Let the Gibbs energies of transfer of electrolytes or ions be known in a mixture of water with non-protogenic organic solvent where OH⁻ is the only lyate ion (e.g., the water-dioxan mixture). For such systems, Eq. (5) is rewritten into the form

$$\Delta G_{t}^{0}(OH^{-}) - \Delta G_{t}^{0}(BPh_{4}^{-}) = \alpha_{s} \left[\Delta G_{t}^{0}(Cl^{-}) - \Delta G_{t}^{0}(BPh_{4}^{-}) \right], \qquad (7)$$

where α_s is the simplified record of coefficient $\alpha(OH, Cl, BPh_4)_s$. Values $\Delta G_t^0(OH^-)$ in such systems are calculated from ionic products of water in mixture (K_s) and in water (K_w) by means of the relation

$$\Delta G_{t}^{0}(\mathbf{OH}^{-}) = 2 \cdot 303 \mathbf{R} T(\mathbf{p} K_{s} - \mathbf{p} K_{w}) - \Delta G_{t}^{0}(\mathbf{H}^{+}).$$
(8)

By inserting Eq. (8) into Eq. (7) we get Eq. (9),

$$2 \cdot 303RT(pK_{s} - pK_{w}) - \Delta G_{t}^{0}(HCl) = (\alpha_{s} - 1) \left[\Delta G_{t}^{0}(Cl^{-}) - \Delta G_{t}^{0}(BPh_{4}^{-}) \right]$$
(9)

from which it is possible to calculate coefficient α_s for the mixtures of water with non-protogenic solvent.

In mixtures of water with protogenic solvent, however, Eq. (7) with the same value of α_s will hold according to the above-mentioned assumption as well but Eq. (8) will take here form (10) with regard to the equilibrium of lyate ions:

$$\Delta G_{t}^{0}(\mathbf{OH}^{-}) = 2.303 \mathbf{R} T(\mathbf{p} K_{s} - \mathbf{p} K_{w}) - \Delta G_{t}^{0}(\mathbf{H}^{+}) + \mathbf{R} T \ln(1 + Q_{1}).$$
(10)

By inserting Eq. (10) into Eq. (7) we get Eq. (11)

$$2 \cdot 303RT(pK_{s} - pK_{w}) - \Delta G_{t}^{0}(HCl) + RT\ln(1 + Q_{1}) = = (\alpha_{s} - 1) \left[\Delta G_{t}^{0}(Cl^{-}) - \Delta G_{t}^{0}(BPh_{4}^{-}) \right].$$
(11)

On comparing Eqs (9) and (11) it is evident that the deviations from linearity defined by Eq. (9) in mixtures of water with protogenic solvent (ROH) are conditioned by term $RT \ln (1 + Q_1)$ in Eq. (11) from which the activity ratio of lyate ions in the given mixture can be calculated.

RESULTS AND DISCUSSION

The proposed method of calculating the activity ratio of lyate ions Q_1 is based on the assumption that there exists the same linear relation between the differences of Gibbs energies of ions (Eq. (5) or (6)) for all solvents or their mixtures. To illustrate this assumption, the dependence can serve of difference of Gibbs energies of transfer $[\Delta G_t^0(\mathrm{Br}^-) - \Delta G_t^0(\mathrm{BPh}_4^-)]$ on the difference of $[\Delta G_t^0(\mathrm{Cl}^-) - \Delta G_t^0(\mathrm{BPh}_4^-)]$. The values of Gibbs energies of transfer for this dependence were taken from literature

Activity Ratios of Lyate Ions

(Marcus¹⁵ and Glikberg and Marcus¹⁶ for pure solvents, Abraham and co-workers¹⁷ for the water-methanol mixture, Wells¹⁸ and Bax and co-workers¹⁹ for water with ethanol, Basu, Kundu²⁰ and Juillard, Tissier²¹ for water with tert-butanol, Wells²² for water and dioxan, Wells²³ for water and dimethyl sulfoxide, Cox and co-workers²⁴ for the water-acetonitrile mixture, and Marcus²⁵ for mixtures of water with alcohols). The dependence mentioned is illustrated in Fig. 1 for 83 pure and mixed solvents (some points in the figure overlap). The validity of Eq. (5) in the considered systems with constant value of $\alpha(Br, Cl, BPh_4)_s = 0.873$ and correlation coefficient r = 0.9949 is evident from Fig. 1.



Fig. 1

The dependence of difference in Gibbs energies of ion transfer $[\Delta G_t^0(Br^-) \Delta G_t^0(\text{BPh}_4^-)$ on the difference $[\Delta G_t^0(\text{Cl}^-) \Delta G_t^0(BPh_4^-)$ in pure solvents [1-propanol (1), acetone (2), propylene carbonate (3), formamide (4), dimethylformamide (5), dimethylacetamide (6), N-methylpyrrolidone (7), nitrobenzene (8), trimethylensulfone (9), hexamethylphosphoric acid triamide (10), 1,1-dichloroethane (11), 1,2-dichloroethane (12)] and in mixtures of water and organic solvent [methanol-water 0, ethanol-water ⊖, 2-propanol-water ⊖, 2-methoxyethanol--water , dioxan-water , ethylene glycol--water \odot , acetonitrile-water \bigcirc , t-butanol--water (), dimethylsulfoxide-water () at 25°C. $X = \Delta G_t^0(Cl^-) - \Delta G_t^0(BPh_4^-), Y =$ $= \Delta G_t^0(\mathrm{Br}^-) - \Delta G_t^0(\mathrm{BPh}_4^-)$





The dependence of difference [2:303RT. $(pK_{\rm S} - pK_{\rm W}) - \Delta G_t^0(\rm HCl)]$ on difference in Gibbs energies of ion transfer $[\Delta G_t^0(\rm Cl^-) - \Delta G_t^0(\rm BPh_4^-)]$ for the binary mixtures water-dioxan \bullet , water-methanol \circ , waterethanol \ominus , water-2-propanol \ominus at 25°C. $X = \Delta G_t^0(\rm Cl^-) - \Delta G_t^0(\rm BPh_4^-), \quad Y = 2:303$, $RT(pK_{\rm S} - pK_{\rm W}) - \Delta G_t^0(\rm HCl)$

Equations (9) and (11) were solved in a similar way. The literature values for the water-dioxan mixture (ionic products²⁶, Gibbs energies of transfer^{22,27-31}) were

TABLE I

The calculated and literature values of the activity ratio of lyate ions Q_1 , individual ionic products of water pK_W and alcohol pK_{ROH} in the mixtures water and alcohol at 25°C

Alcohol	Literature values of Q_1					
(wt. %)	Gaboriaud	Rochester		Q ₁	pK _W	р <i>К</i> _{ROH}
Water-methanol						
10.00	·09 ^a	·11 ^b	·11 ^c	·36	14.17	14.62
20.00	$\cdot 30^a$	$\cdot 26^{b}$	·26 ^c	·90	14.33	14.38
30.00	· 58ª			1.70	14.50	14.27
40.00	$1 \cdot 20^a$			3.02	14.68	14.20
50.00	1·95 ^a	$1 \cdot 06^{b}$	1.16 ^c	4.94	14.87	14.18
60.0 0	$2 \cdot 80^{a}$	1·59 ^b	1.82 ^c	8.32	15.10	14.18
70.00	3·90ª	2.51^{b}	2·97°	13.64	15.38	14.25
80.00	6.50 ^a	$4 \cdot 54^{b}$	5.69°	22.26	15.79	14.44
90.00	14·50 ^a	12·75 ^b	13·26 ^c	40.27	16.10	14.50
		Water-	ethanol			
10.00	·18 ^d	·23 ^d		·04	14.21	15.74
20.00	•46 ^d	·52 ^d		·10	14.37	15.73
30.00	1·87 ^d	·89 ^d		·27	14.60	15.18
40.00				·51	14.82	15.11
50.00		1·91 ^d		·78	15.07	15.18
60.00				1.21	15.34	15.26
70 ·00				1.69	15.72	15.49
80.00				2.66	16.21	15.79
9 0·00				4.75	16.96	16-28
		Water-2-	propanol			
10.00	·18 ^d	·40 ^d		·0 2	14.28	15.94
20.00	·65ª	·89ª		·06	14.55	15.75
30.00	2·53 ^d	1·34 ^d		·13	14.76	15.64
40.00				·30	15.02	15.55
50· 0 0	12·78 ^d	1·68 ^d		· 39	15.29	15.70
60.00				·50	15.61	15.91
70.00				•53	16.12	16.39

^a Ref.¹¹, ^b ref.², ^c ref.¹², ^d ref.⁹.

used for calculating coefficient $\alpha(OH, Cl, BPh_4)_s = 1.1$. To calculate the ratio of lyate ions Q_1 , the literature values of quantities needed were used as well, their values reported by more authors being averaged or interpolated (for the mixture of water with methanol^{1,17,28,32-39}, with ethanol^{1,9,18,19,26,28,40-43}, with 2propanol^{1,9,20,26,28,40,44-47}). The dependence of the left-hand side of Eq. (9) on the difference of Gibbs energies of transfer $[\Delta G_t^0(Cl^-) - \Delta G_t^0(BPh_4^-)]$ is shown in Fig. 2. The deviations from linear dependence are caused by term $RT \ln (1 + Q_1)$ which appears in Eq. (11) for protogenic mixtures. The values of Q_1 given in Table I along with the literature ones^{2,9,11,12} were calculated from these deviations. For the sake of completeness, the calculated individual ionic products of water pK_W and alcohol pK_{ROH} in the systems studied are given in Table I.

For the water-methanol system, the differences between the literature values^{2,11,12} and calculated Q_1 are evident from Table I. However, the given results are linearly dependent each other so that experiment should decide their rightness. In the systems of water with ethanol and 2-propanol, the literature values⁹ are not mutually comparable and with regard to the results of kinetic studies^{3,4}, they seem to be too high in comparison with the water-methanol system. On the contrary, the values calculated here comply with the qualitative anticipation that the ratio of activities of lyate ions in mixture will decrease, too, with decreasing polarity of organic component.

The proposed method makes it possible to calculate Q_1 in the media where the hitherto used methods^{2,9,11,12} have not been successful, and it is also less demanding as to the input information. In comparison with the method by Rochester², it does not require the knowledge of activities of both components of solvent which are not always available. Its accuracy is connected with the accuracy of experimental determination of differences in the Gibbs energies of ion transfer and ionic products pK_s . The calculation will be subject to a great error for small values of Q_1 so that the calculation will be difficult for the mixture of water with slightly polar organic solvent. For more polar organic solvents, the method may provide satisfactory results.

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